DEVELOPING A MODEL TO PREDICT CORPORATE BANKRUPTCY USING DECISION TREE IN THE REPUBLIC OF SERBIA

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Abstract. Decision trees made by visualizing the decision-making process solve a problem that requires more successive decisions to be made. They are also used for classification and to solve problems usually addressed by regression analysis. One of the problems of classification that arises is the proper classification of bankrupt companies and non-bankruptcy companies, which is then used to predict the likelihood of bankruptcy. The paper uses a random forests decision tree to predict bankruptcy of companies in the Republic of Serbia. The research results show the high predictive power of the model with as much as 98% average prediction accuracy, and it is recommended for auditors, investors, financial institutions and other stakeholders to predict bankruptcy of companies in Republic of Serbia.

Key words: decision trees, bankruptcy, prediction, model

JEL Classification: C44, C53, G33

1. INTRODUCTION

A quantitative method that iteratively detects links between attributes, data subject to testing, is called data mining. Data mining relies on decision trees that visualize the decision-making process to solve a problem that requires several successive decisions (Sikavica, et al., 2014, p. 476). Decision trees are often used to solve classification problems, i.e. to determine belonging to a particular class, and to solve regression problems.
One of the classification problems is the proper classification of bankruptcy and non-bankruptcy companies, thus making a prediction of corporate operations. Identifying business difficulties that lead to bankruptcy is a core task for numerous stakeholders. Banks, managers, investors, customers, suppliers avoid major losses by timely discovering unstable operations leading to bankruptcy. However, forecasting bankruptcies under current business conditions has become an increasingly significant challenge for analysts due to the globalization and complexity of companies, as well as the fact that certain economists perceive the initiation of bankruptcy as a strategic solution for the limitation of liability arising from court-imposed penalties (Kliestik et al., 2018). Various bankruptcy prediction models have been developed bearing in mind the significance of bankruptcy forecasting to numerous market participants and factors that affect the forecasting accuracy. Decision trees are categorized as contemporary models which, based on input data (numeric and categorical), predict bankruptcy.

The remainder of this paper is structured as follows. First, the theoretical and methodological basis of the decision tree is given, as well as an overview of some of the models used to predict bankruptcy. The advantages and disadvantages of the decision tree are highlighted as well as the previous research results in this area. Finally, a decision tree is implemented to predict corporate bankruptcy in Republic of Serbia. An overview of the influence of individual variables on the prediction result is also given.

2. THEORETICAL AND METHODOLOGICAL BASES OF MODELS FOR CORPORATE BANKRUPTCY PREDICTION USING DECISION TREE

Decision trees can be a graphic overview of decision making by experts based on a hand-created tree. In addition to the expert’s decision, decision trees can rely on data finding its mutual links to obtain predictive values. Such trees are called Classification and Regression Trees (CART) and were developed by a group of American statisticians, Breiman, Friedman, Olshen, and Stone (1984). The goal of classification trees is to assign attributes to a subset of known classes. Specifically, the attribute space is divided into several different regions that do not overlap. A new object is determined to belong to one of the regions based on the values of the attributes describing the object (for example, corporate business operations are described by financial ratios). The object will be assigned to the class that dominates the region in which the object is located (James, et.al. 2013 p. 311) (for example, the class may be to continue business or go bankrupt).

The regression trees were developed in a similar way to the classification trees, except that the result of the analysis does not represent belonging to a class but an approximation of an unknown regression function. Regression trees are estimated using non-parametric regression functions (Härdle & Simar, 2007, 401).

The decision tree is based on recursive, binary splitting data, moving from a higher (tree) to a lower (leaf) level. Each tree node represents one test of the input attribute (variable) value, and each branch stemming from the node shows one of the possible attribute values. A leaf represents a class to which subset attributes belong (Stanojević, et al. 2017 p. 94). The tree is then formed by splitting the input dataset into subsets based on data value testing. The figure 1 shows a decision tree for predicting company bankruptcy, classifying each company as succeeding or failing. Assuming one of the attributes is ratio
1 – working capital/total assets, then the first splitting rule is to branch the tree into two sides, as follows (Gepp & Kumar, 2015, p. 398):

- “Left sub-tree, if ratio is 1 ≤ 0,11, or
- Right sub-tree, if ratio is 1 > 0,11”.

![Decision Tree Diagram](source)

**Fig. 1** An example of a decision tree classifying company operations


In addition to classification and regression trees (CART), there are other popular algorithms that use top-down recursive data splitting, such as ID3 (Quinlan, 1986) and C4.5 (Quinlan, 1993). In the decision tree development process, the C4.5 and CART algorithms include two conceptual phases, namely: the growth phase and the tree pruning phase. Other algorithms only apply the growth phase when developing the decision tree.

Methods such as bagging, random forests and boosting methods are often used when developing the decision tree. The paper uses the random forests method, which is an advanced bagged decision tree. The difference to the bagged tree is that the modified decision tree algorithm “at each candidate split in the learning process selects a random subset of features” (James, et al. 2013 p.319).

3. AN OVERVIEW OF STUDIES ON THE USE OF THE DECISION TREE TO DEVELOP BANKRUPTCY PREDICTION

Unlike the frequent use of neural networks to predict corporate bankruptcy, researchers in the field of economics do not widely use decision trees. Although the first model was developed back in 1985, studies scarcely address the decision tree application to predict corporate bankruptcy.

1) Halina Frydman, Edward Altman, and Duen-Li Kao (1985) were the first to apply the decision tree, as a non-parametric model, to predict corporate bankruptcy and circumvent assumptions imposed by discriminant analysis and logistic regression. They used a recursive partitioning algorithm to develop a decision tree. The sample consisted of 58 bankrupt
companies and 142 active manufacturing and trading companies. The survey covered the period from 1971 to 1981. The authors used 20 financial ratios they considered significant for predicting bankruptcy in previous studies.

In relation to the number of input variables, the authors developed 2 decision tree models (larger, more complex, and smaller, simpler decision trees) and 2 models based on discriminant analysis (one model containing 4 and one with 10 variables). The research results showed the superiority of the decision tree model over the discriminant analysis models. In line with expectations, smaller decision tree showed better results, while complex decision trees highlighted the potential risk of over-training and poorer predictive results.

2) Thomas E. McKee (1995a) implemented the ID3 inductive inferencing algorithm to predict the bankruptcy of 60 US publicly traded companies. Half of the sample companies were bankrupt companies and the other half were active companies. The survey covered the period from 1986 to 1989. The input variables were 8 financial ratios (McKee, 1995a, p. 30):

- “Net income/Total assets
- Working capital/Total assets
- Current assets/Current liabilities
- Cash/Total assets
- Current assets/Sales
- Long-term debt/Total assets
- Accounts receivable/Sales revenue”.

As the final research result, the author proposed a bankruptcy prediction model containing only two financial ratios, namely: current assets to current liabilities ratio and net income to total assets ratio. The model showed to predict the sample company bankruptcy with 97% accuracy. The author notes that the model should be tested using a larger sample, but still recommends auditors, investors and other stakeholders to use the model to predict bankruptcy.

In the same year, the author McKee (1995b) developed a recursive partitioning algorithm to predict bankruptcy, with the rule that if the current liquidity ratio was greater than or equal to 0.64 and the ratio of net income to total assets greater than or equal to 0, then the company will not file for bankruptcy, otherwise it is believed that the company will file for bankruptcy. The model was developed and tested using a sample of 202 companies, half of which were bankrupt and the other half actively operating. A few years later, McKee and Greenstein (2000) tested the robustness of the same model using an extended sample over a different time period and with different data. The results of the study showed that the developed model had a higher average percentage of prediction accuracy than the logit model and the neural network model. However, when it comes to predicting bankrupt company bankruptcy, the developed model showed less predictive power than the other models examined.

3) Adrian Gepp, Kuldeep Kumar, and Sukanto Bhattacharya (2010) extended the Frydman et al. research, applying different decision tree algorithms to predict corporate bankruptcy. In addition to the recursive partitioning algorithm, the authors implemented the CART and See5 algorithm. They compared the results of different decision trees, but also compared the results of the decision tree with the discriminant analysis model. Interestingly, the authors conducted a survey using the sample used by Frydman et al, with the same number of input variables.
 Algorithms play a role in managing the decision tree development process, with two main tasks (Gepp, et.al. 2010 p. 540):

- Selection of the best splitting rule of data at each node distinguishing between active and bankrupt companies, and
- Managing the complexity of the decision tree (number of nodes). Many algorithms first develop a very complex tree, and then prune it to the desired complexity.

The results of the study confirmed the results of previous studies that smaller and simpler decision tree models “are better predictors than more complex models” (Gepp, et.al. 2010 p. 546). The authors emphasize that the recursive partitioning algorithm is a superior classifier and predictor of corporate bankruptcy. On the other hand, the See5 algorithm showed the best classification ability but also the worst predictive power. The CART algorithm showed very similar results to the recursive partitioning algorithm. Compared to the discriminant analysis model, all decision tree models showed their superiority.

4. ADVANTAGES AND DISADVANTAGES OF CORPORATE BANKRUPTCY PREDICTION MODELS USING DECISION TREE

„Decision trees are powerful classification algorithms that are becoming increasingly popular due to intuitive explanatory features“ (Olson, et al. 2012 p. 466). Nayab (A Review of Decision Tree Analysis Advantages, Retrieved from: https://www.brighthubpm.com/project-planning/106000-advantages-of-decision-tree-analysis/, 11/08/2019) summarized the benefits of a decision tree in several points:

- Transparency – Decision trees explicitly provide all possible alternatives and present each alternative to a final conclusion, thus enabling alternatives to be compared;
- Specificity – The ability of the decision tree to assign certain values to the decisions (problem) and results of each decision, thereby reducing ambiguities in decision making;
- Comprehensiveness – Decision trees provide a comprehensive analysis of the consequences of any decision that may end with a definitive conclusion, uncertainty or lead to new issues that require a repeat of the process;
- Ease of use – Decision trees provide a graphical representation of problems and alternatives in a simple and easy to understand format that requires no further explanation;
- Flexibility – The ability of the decision tree to handle different types of data (value and categorical);
- Resilience – Decision trees focus on the relationship between different events, depicting the natural course of events. That way, they remain robust to error, provided the input is correct;
- Confirmation – Decision trees are used as a quantitative analysis of problems in corporate operations, but also for validation of the results of statistical tests.

Because of their structure, decision trees are believed to be similar to human decision making, and graphical representation facilitates interpretation, especially with small trees. The ability to manage qualitative predictors does not require the introduction of dummy variables (James, et al. 2013 p. 315).

Developing a decision tree is possible by applying different algorithms, which have their advantages and disadvantages. One of the most famous algorithms for generating a
decision tree is the ID3 algorithm. Noting the shortcoming of an original decision tree, reflected in dealing with noisy and/or incomplete data, Quinlan (1986) compares two ways to modify methodology and overcome the shortcoming by introducing a new algorithm.

Quinlan (1987) investigated four methods for simplifying decision trees in a way that does not compromise predictive accuracy to ensure ease of use. The author concludes that the „pessimistic pruning method is faster than other applied methods and does not require a special test sample for validation“. At the same time, the author states that the reduced error pruning method requires a separate test sample, and another weakness of the method is that parts of the original tree that are less frequent and specific cases are not presented in the test sample and can be cut. Finally, the author concludes that the simplifying to production rules method has proven particularly powerful.

Nayab found disadvantages of the decision tree (A Review of Decision Tree Disadvantages. Retrieved form: https://www.brighthubpm.com/project-planning/106005-disadvantages-to-using-decision-trees/, 11 August 2019) in the following features:

- Instability – Reliability of information in the decision tree depends on the accuracy of the input data. Even a small change in data entry can cause major changes in the tree, which may require the development of a new tree;
- Complexity, Unwieldy – Although the decision tree is easy to use compared to other models, developing a decision tree is a complex and time-consuming process. Complexity is particularly pronounced in large trees with many branches, and expertise and experience are crucial to solving such problems. Large trees are often cumbersome, leading to difficulties and incomprehensibility in their presentation;
- Costs – As already mentioned, developing large trees requires human training and expertise, and training costs for using a decision tree are imposed as a necessity;
- Information overload – Although decision trees are capable of generating large amounts of data, which is considered a positive feature, it may sometimes be that decision makers face a wealth of information. In these circumstances, it takes time for the decision maker to process all the data, making the decision-making process time-consuming and costly.

Compared to other regression and classification approaches, the decision tree generally does not have the same level of prediction accuracy. However, by modifying the decision tree by introducing different methods such as bagging, random forests, and boosting, predictive power significantly improves (James, et al. 2013 p. 316).

Kim and Upneja (2014) used a decision tree and an adaboosted decision tree to examine the key factors for the financial failure of a publicly traded restaurant in the US. The authors found that restaurants with financial problems had a higher share of debt in the capital structure, a lower rate of increase in assets, a lower profit margin, and a lower current liquidity ratio than restaurants that were not financially disadvantaged. Due to the good performance of predicting business failure, the authors recommend using an adaboosted decision tree.

In the credit rating evaluation, Bastos (2008) applied a boosted decision tree. Considering that the boosted decision tree outperformed multilayer perceptron and the support vector machines, the author concludes that the model is competitive with other credit rating models.

Shirata (1998) applies classification and regression trees (CART) to select the variables that will be used in the discriminant analysis model to predict the bankruptcy of
Japanese companies. Using CART, it is possible to calculate significance for each variable. In order to predict the bankruptcy of Huarng, Yu and Chen (2005) applied CART and demonstrated its superiority over other models. The main objection to their research is that the sample included only 12 companies and 5 variables. Li, Sun and Wu (2010) also confirmed the superiority of CART, highlighting the positive sides reflected in ease of application and results, accuracy and stability, non-linear estimation and non-parametric model. Durica et al. (2019) applied the CARD and CHAID decision tree algorithm to predict the bankruptcy of Polish companies, whereby the average prediction accuracy of the final models was 97.9% for the CART model and 98.2% for the CHAID model. Application simplicity, handling of missing data and easy interpretation of results were the most prominent advantages of these models.

Cha and Tappert (2009) applied a genetic algorithm to make decision trees compact and near-optimal. By limiting the height of the tree, the authors state that the derived model offers the same or better results than the best known algorithms.

Although they prefer to use the decision tree to predict corporate bankruptcy over logistic regression models, neural networks and support vector machines, Olson et al. state that comprehensibility, as a major advantage of the decision tree, is undermined by too many rules in developing the tree itself. Avoiding this problem is possible by controlling the „number of rules obtained from decision tree algorithms to a certain degree, by setting different minimum levels of support“ (Olson, et al. 2012 p. 464).

5. IMPLEMENTATION OF THE DECISION TREE TO DEVELOP BANKRUPTCY PREDICTION MODELS OF MANUFACTURING AND TRADE COMPANIES IN THE REPUBLIC OF SERBIA

For the research purposes, a sample of 204 (large and medium-sized) manufacturing and trade companies operating in the Republic of Serbia was formed. Half of the sample companies are bankruptcy companies from 2011 to 2017. The other half is made up of non-bankruptcy companies, timed with those in bankruptcy. Companies that initiated bankruptcy proceedings were selected on the basis of a list of active bankruptcy proceedings published by the Bankruptcy Licensing Agency (Bankruptcy Statistics, 2018). Non-bankruptcy companies are those that continuously and unhindered carry out their business activity, matched by industry (manufacturing and trade companies) and asset size with bankruptcy companies, selected from the database of the Business Registers Agency (Unified Search, 2018).

The total sample is divided into two parts. One part represents the training sample and is used for model development, while the other part is the validation sample and is used to control, i.e. to check the predictive power of the developed model (Banasik, Crook, & Thomas, 2003). The largest part of the total sample should be related to the model construction, and it is accepted in practice that this ratio can be 80:20 or 70:30 in favor of the training sample (Nikolić, et al. 2013). 80:20 ratio, 42 companies in validation sample and 162 companies in training sample were used in the paper.

Based on previous studies dealing with the corporate bankruptcy prediction, 56 initial variables were selected. After a t-test that eliminated variables that did not significantly influence bankruptcy prediction and eliminated multicollinearity, there were 15 variables left to use to develop the decision tree:
The paper uses a random forests decision tree. The results of the accuracy of bankruptcy prediction of the analyzed companies are presented in Table 1.

### Table 1 Bankruptcy prediction using a random forests decision tree

<table>
<thead>
<tr>
<th>Companies</th>
<th>Precision</th>
<th>Recall</th>
<th>F1-score</th>
<th>Support</th>
</tr>
</thead>
<tbody>
<tr>
<td>Bankruptcy</td>
<td>0.95</td>
<td>1.00</td>
<td>0.98</td>
<td>21</td>
</tr>
<tr>
<td>Non-bankruptcy</td>
<td>1.00</td>
<td>0.95</td>
<td>0.98</td>
<td>21</td>
</tr>
<tr>
<td>Avg / total</td>
<td>0.98</td>
<td>0.98</td>
<td>0.98</td>
<td>42</td>
</tr>
</tbody>
</table>

Source: Authors’ calculations

Precision is a measure of the success of a classifier that shows the percentage that actual bankruptcy companies make relative to all companies designated as bankruptcy companies. Based on Table 1, it can be concluded that the decision tree correctly classified 95% of bankruptcy companies in relation to the number of companies designated as bankruptcy. Also, it can be concluded that all actual non-bankruptcy companies are properly classified in relation to companies designated as non-bankruptcy.

Recall is a classifier performance measure that shows what percentage of companies are classified as bankruptcy relative to all companies that are truly bankruptcy. The survey results show that the decision tree classified all bankrupt companies in the bankruptcy class. However, some non-bankruptcy companies were also classified into bankruptcy class.

The F1-score is a measure of the success of a qualifier that combines precision and recall allowing a simpler comparison of different algorithms. The F1-score gives equal importance to precision and recall and is 0.98 equal to the average accuracy of predicting bankruptcy of a company using a decision tree.

As compared to the results of the study conducted by Stanišić et al. (2013) who, by comparing the predictive power of models based on discriminatory and logit analysis, neural networks and decision trees, found that decision trees had accurately classified 49 of 65 bankrupt and active companies (75.4% accuracy), our results show a far greater predictive power of the decision tree.
The results obtained are in line with the Bastos (2008) study, which established a generalization accuracy of 94.03% for Australian data using boosted decision trees. Largely similar results were obtained by Durica et al. (2019) who established an average accuracy of the bankruptcy prediction model in cases of Polish companies of 97.9% for the CART and 98.2% for the CHAID decision tree.

Berent et al. (2017) consider that the focus of research has shifted from maximizing the accuracy of predictive models to analyzing the informational significance of individual predictor variables. Berent et al. (2017) consider that the focus of research has shifted from maximizing the accuracy of predictive models to analyzing the informational significance of individual predictor variables. Depending on the business conditions, explanatory variables in models vary from country to country (Kovacova et al., 2019). Thus observed, the specifics of individual activities may also affect the selection of variables. Using the decision tree, the relative importance of variables in bankruptcy prediction first for all sample firms and then individually for manufacturing and trading companies was examined.

Figure 2 shows three variables affecting the prediction result by more than 15%. These are the following:
- \( \frac{\text{EBIT} + \text{amortization}}{\text{Interest expense}} \)
- \( \frac{\text{Net income}}{\text{Sales}} \)
- \( \frac{\text{Net income}}{\text{Total assets}} \).

Profitability and indebtedness had the greatest average impact on the bankruptcy prediction of the sample companies. However, if only manufacturing companies are observed, the variables that have the greatest impact on the prediction result also change, as Figure 3 shows.
Fig. 3 Average variable impact on the prediction result of manufacturing companies

The highest average impact on the bankruptcy prediction of manufacturing companies is the ratio of net income to sales, with more than 17%. It is followed by indicators of indebtedness, profitability and liquidity.

Figure 4 shows the average impact of variables on bankruptcy prediction of trading companies.

Fig. 4 The average variable impact on prediction result of trading companies

Figure 4 shows that the same variables (the first three) have the greatest average influence on the prediction result of trading companies, when looking at the total sample. Significant variables include liquidity ratios.
The variable that has proven significant for bankruptcy in all companies is the net income and total assets ratio, which is one of two variables used by McKee (McKee, 1995b; McKee & Greenstein, 2000) in their decision tree models to predict bankruptcy. Net income to total assets ratio is the most commonly used variable in bankruptcy prediction models (Bellovary, et al. 2007 p. 42)

6. CONCLUSION

The need to predict the business failure of a company facing bankruptcy proceedings has led researchers to search for a model that will most accurately predict future business. From discriminant analysis, logistic regression, to neural networks and various hybrid models, new models that may be the most appropriate to predict the bankruptcy of companies operating in a specific economic environment are constantly emerging.

Compared to traditional bankruptcy prediction models (discriminatory, logit and probit models), decision trees have a number of advantages, which are reflected in the simplicity of implementation, easy interpretation of results, handling of different data types and overcoming data deficiency issues. Flexibility and customization enable using decision trees to predict the bankruptcy of companies operating in different economies. In addition, the differences in predicting bankruptcies of companies engaged in various activities are perceived with ease.

However, the underlying issues appearing upon the application of a decision tree arise from its instability, where even slight alterations of input data may lead to a significant change in the tree and its prediction power. A relatively broad data sample is desirable for tree development; otherwise, there is a risk of quick overfitting (Weissova et al., 2016). Understandability, as one of the advantages of using decision trees, may be undermined by too many rules related to tree development; this may be avoided by controlling the number of rules by setting up various minimum support levels.

The paper uses a random forests decision tree to predict bankruptcy of companies in Republic of Serbia. The research results show the high predictive power of the model with as much as 98% average prediction accuracy, and it is recommended for managers of companies and financial institutions, investors, the Bankruptcy Licensing Agency, as well as other stakeholders in predicting the bankruptcy of a particular company in the Republic of Serbia.

REFERENCES


Stabla odlučivanja vizuelizacijom procesa odlučivanja rešavaju problem koji zahteva donošenje više sukcesivnih odluka. Često se koriste i za rešavanje problema klasifikacije i regresije. Jedan od problema klasifikacije koji se pojavljuje jeste pravilno klasifikovanje preduzeća u stečaju i aktivnih preduzeća, na osnovu čega je moguće predviditi verovatnoću pokretanja stečaja. U radu je primenjeno random forests stablo odlučivanja za predviđanje stečaja preduzeća u Republici Srbiji. Rezultati istraživanja pokazuju visoku prediktivnu moć modela sa čak 98% prosečne tačnosti predviđanja, te se preporučuje njegovo korišćenje revizorima, investitorima, finansijskim institucijama i ostalim stakholderima za predviđanje stečja preduzeća u Republici Srbiji.

Ključne reči: stabla odlučivanja, stečaj, predviđanje, model